Experimental Heat Transfer and Pressure Drop Studies in Packed Bed Columns with Nanofluids

G. Srinivasa Rao

Department of Mechanical Engineering, Kakatiya Institute of Technology and Science, Warangal-506015, India . *Corresponding author e-mail: gsrkits@gmail.com

Abstract - Various manufacturing and process industries use packed bed columns to transfer heat. The heat transfer mainly depends on bed void fraction, bed material and the properties of the fluid. Conventional liquids such as water have higher heat transfer coefficients compared to gases such as air. Nanofluid is a liquid dispersed with metal and metal oxide particles of nanometer size in a base liquid such as water. The nanofluids show a significant increase in the values thermal conductivity which increases with the concentration and temperature. At low values of concentration and operating temperature of about 35°C, experiments with nanofluids indicate higher heat transfer rates when compared to water. Equations are available for the estimation of Nusselt number and pressure drop for different conditions of flow of conventional fluids in tubes and conduits. Equations developed can be used for the estimation of heat transfer of nanofluids through packed bed columns. The salient outcomes of the state of art of research in packed beds listed.

Keywords: packed bed, nanofluid, heat transfer, pressure drop ,friction factor

INTRODUCTION

The heat transfer in a packed bed takes place between the liquid and packed material. The heat transfer through packed beds has wide applications in chemical and process industries. The analysis of experimental heat transfer coefficients and pressure drop is for flow of nanofluid through a packed bed column. However, such experiments with nanofluids have not been reported till now. The present work outlines the key characteristic of heat transfer and pressure drop undertaken with conventional fluids such as air and water. The determination of heat transfer coefficient and pressure drop is for flow of nanofluids in packed bed columns.

2.0 Determination of Pressure Drop And Heat Transfer

The friction factor for flow of fluid in a packed bed column is determined from the relation

$$f = \frac{\Delta P}{L_b} \frac{D_P}{\rho V_s^2} \left(\frac{\varepsilon^3}{1 - \varepsilon} \right) \qquad (1)$$

The equation of Ergun [7] is used for the estimation of pressure drop given by

$$\Delta P = \frac{150\mu V_s L_b}{D_p^2} \frac{(1-\epsilon)^2}{\epsilon^3} + \frac{1.75\rho V_s^2 L_b}{D_p} \frac{(1-\epsilon)}{\epsilon^3}$$
(2)

where \mathcal{E} is the bed void fraction and can be determined from the relation $\epsilon = 1 - V_p / V_b$, in which V_p and V_b are volume of particles and volume of bed respectively. V_s is superficial velocity D_p is particle equivalent diameter given in the form $D_p = 6V_p/S_p$ and S_p is surface area of the particle. The experimental pressure drop is calculated with the equation given by

$$\Delta P_{exp} = R_{m} (\rho_{A} - \rho_{bf}) g/g_{c}$$
(3)

The pressure drop estimated with Eq.(1) for different flow rates are compared with the experimental values and presented in the form of graphs. Theoretical and experimental friction factors are calculated by using the Ergun[7].The early works on packed bed heat transfer are due to Anzelius [1], although Schumann [21], is usually cited in most studies. Both the authors assumed the fluid to be incompressible, and obtained expression for the evaluation of heat transfer coefficient. They assumed the fluid to flow uniformly through a bed of solid particles with perfect conductivity between the particles. The derived heat transfer equation is given by

$$T_{s} = (T_{fi} - T_{si}) \int_{0}^{\infty} I_{0} (2\sqrt{YZ}) e^{-Y} e^{-Z} dZ + T_{si}$$
(4)

Equation (1) can be modified and written as

$$T_{f} - T_{s} = (T_{fi} - T_{si})I_{0}(2\sqrt{YZ})e^{-Y}e^{-Z}$$
(5)

$$\frac{\mathbf{T}_{f} - \mathbf{T}_{s}}{\mathbf{T}_{fi} - \mathbf{T}_{si}} = \mathbf{I}_{0} \left(2\sqrt{\mathbf{Y}Z} \right) e^{-\mathbf{Y}} e^{-Z} \quad (6)$$



Where
$$\mathbf{Y} = \frac{\mathbf{h}_{f} \mathbf{a} z}{\rho_{f} \mathbf{C} \mathbf{p}_{f} \mathbf{V}_{f}}$$
 and $\mathbf{Z} = \frac{\mathbf{h}_{f} \mathbf{a} \theta}{\rho_{f} \mathbf{C} \mathbf{p}_{f} (1-\varepsilon)}$ (7)

The solutions of these equations presented in graphical from are called Schumann curves. Furnas [8] extended the Schumann curves to a wide range of temperatures. An empirical relation for the evaluation of the heat transfer coefficient developed is given by

$$h_{V} = \frac{AG^{0.7}T^{0.3}10^{\left(0.6\&-3.56\epsilon^{2}\right)}}{D_{p}^{0.9}}$$
(8)

Saunders and Ford [22] used dimensional analysis to obtain an equation for the estimation of heat transfer coefficients. The research was however limited to spheres and cannot be applied to other geometries of solid particles. Kays and London [10] presented a correlation for the evaluation of heat transfer coefficients between a gas and randomly packed solid spheres with the Colburn j- factor. The correlation equation given is

 $j_{H} = 0.23/\text{Re}_{p}^{0.3} j_{H} = \text{StPr}^{0.66}$ for (9) (200<Re_p<50,000and0.37< ϵ <0.39)

Lof and Hawley [14] investigated the heat transfer between air and packed bed of granite gravel. The unsteady state heat transfer was correlated with air mass velocity and particle diameter valid in the range of $8 < D_p < 33 \text{ mm}$

 $0 < \text{Re}_p < 500 \text{ and } 311 < T_b < 394 \text{K}$. The equation obtained is given by

(10)

8.ering

$$h_{\mathbf{V}} = 0.652 \left(\frac{G}{D_{\mathbf{P}}}\right)^{0.7}$$

Leva [13 -15] determined the heat transfer coefficient between smooth spheres of low thermal conductivities of size 6.8 mm and fluids (air and carbon dioxide) in packed beds and tubes (column) diameters of 50.8mm. The ratio of particles to tube diameters D_P/D_t was varied from 0.008 -0.27. Fluid flow rate was of Reynolds number range 250 – 3000. Correlation of film coefficient was found to be

$$h = 3.50 (k/D_t) Exp \left[-4.6 (D_P/D_t) (D_P G/\mu)^{0.7} \right] (11)$$

And a modified form is given as

$$h = 0.40 \frac{k}{D_t} \left(\frac{D_P G}{\mu} \right)^{0.7}$$
(12)

Ball [2], Norton [17], Meek [15], Bradshaw et al. [4] has worked on various packed beds using air and other gases as fluids and developed correlations for heat transfer coefficient. Barker [3] has given extensive reviews on these works and compared the results obtained by these authors. Baldwin [5] has developed correlations for the estimation of heat transfer of water flowing through bed of spheres in the range 3000<Re<70,000 for regular cubic arrangement having a void fraction of $\varepsilon = 0.47$

$$j_{\rm H} = 0.992/{\rm Re}^{0.33}$$
 (13)

for dense cubic arrangement having $\varepsilon = 0.261$ as $0.940 \text{Re}^{0.30}$ (14)

Shen *et al.* [23] performed experiments at low values of Reynolds number in the range of 5 to 229 with 1.3 and 2.7mm glass beads packed inside a 63 mm diameter polystyrene cylinder. Based on their experimental observations, they observed that the correlation developed by Gunn [9] could predict their data for a wide range of porosities between 0.35 and 1.0 and Reynolds numbers up to 10^5

$$Nu = \frac{hD_{P}}{k_{f}} = 7 \quad 10\varepsilon + 5\varepsilon^{2} \qquad 1 + 0.7Re_{P}^{0.2}Pr^{1/3} + 2.4\varepsilon + 1.2\varepsilon^{2} \quad Re_{P}^{0.7}Pr^{1/3}$$
(15)

Wakao *et al.* [25] have presented a correlation that is corrected for axial fluid thermal dispersion

$$Nu = \frac{hDp}{k_{f}} = 2 = 1.1 \text{Re}_{p}^{0.6} \text{Pr}^{0.33}$$

for 15 < Re_p < 8500 (16)

Nsofor and Adebiyi [16], when referring to Wakao *et al.* [25] presented similar equation as

$$Nu = \frac{hDP}{k_{f}} = 2 + 1.1[6(1 - \varepsilon)]^{0.6} Re_{P}^{0.6} Pr^{1/3}$$
(17)

while Schroder *et al.* [20] used the structure of the equation given by Wakao *et al.*, Dixon and Cresswell [6] pursued a theoretical model for the prediction of heat transfer in radial fluid flow in packed beds. The correlation suggested by them is valid for Rep >100 and a bed to particle size ratio >

$$Nu = \frac{hD_p}{k_f} = \frac{0.255}{\epsilon} Re_P^{0.67} Pr^{1/3}$$
(18)

 k_f is the fluid thermal conductivity. The experimental investigation undertaken by various authors is presented next.

III. The Physical Properties of Nano Fluids

The density and specific heat of nanofluid at different volume concentrations are estimated using the following relations valid for homogeneous mixture given by

$$\rho_{nf} = \phi \rho_p + (1 - \phi) \rho_{bf} \tag{20}$$

$$C_{p_{nf}} = \frac{(1-\phi)(\rho C_{p})_{bf} + \phi(\rho C_{p})_{p}}{(1-\phi)\rho_{bf} + \phi\rho_{p}}$$
(21)

The experimental data of viscosity available in literature for Cu, CuO, Al₂O₃, TiO₂, SiO₂, ZrO₂, ZnO nanoparticles dispersed in water is subjected to regression by Sharma et al. [2012] for $0 \le \phi \le 3.7$, $20 \le T_b \le 70$, $20 \le d_p \le 170$. The equation is obtained with a deviation



of less than 10% where ϕ is in percent, T_b in 0 C and d_p in nm as

$$\frac{\mu_{nf}}{\mu_{w}} = C_1 \left(1 + \frac{\phi}{100} \right)^{11.3} \left(1 + \frac{T_{nf}}{70} \right)^{-0.038} \left(1 + \frac{d_p}{170} \right)^{-0.061}$$
(22)

 $C_1 = 1.4$ for SiC nanofluid and $C_1 = 1.0$ for other water based nanofluids.

Different models for the determination of effective thermal conductivity of two phase solid-liquid mixtures are developed from the classical Maxwell [29] equation given as

$$k_{eff} = k_{bf} \left[\frac{k_p + 2k_{bf} + 2\phi(k_p - k_{bf})}{k_p + 2k_{bf} - \phi(k_p - k_{bf})} \right]$$
(11) Vajjha

and Das [28] proposed the following equation to estimate thermal conductivity of

$$k_{nf} = \frac{k_{p} + 2k_{f} + 2(k_{p} - k_{f})\varphi}{k_{p} + 2k_{f} - (k_{p} - k_{f})\varphi} k_{f} + 5 \times 10^{4} \beta \varphi \rho_{f} C p_{f} \sqrt{\frac{k_{p}T}{\rho_{p}d_{p}}} f(T,\varphi)$$
(23)

Sharma et al. [30] developed an equation for the determination of thermal conductivity of Cu, CuO, Al_2O_3 ,

3.0 Experimental Review on packed bed heat transfer

TiO₂, SiO₂, ZrO₂, ZnO nanoparticles dispersed in water valid in the range $0 \le \phi \le 3.7$, $20 \le T_b \le 70$, $20 \le d_p \le 170$. The equation is obtained as



Author	System	Method of heating	Range of Reynolds number (Re _P) used	Correlation
Baumeister and	Air- Steel	Electrical induction	2 <mark>00</mark> – 10400	$j_h = 1.09 Re_P$
Bennet (1958)		(Steady state)		
Bradshaw and	Air –celite	water soaked packing's	<mark>30</mark> 0 − 2500	$j_h = 2.52(Re_P)^{0.5}$
Mayer (1963)	cylinders, etc	dried by air at room temperature		
Bunnel et.al	Air –alumina	Heated airbed wall	30 - 150	$K_{er}/K_{ef} = 5.0+0.061 Re_P$
(1949)		Maintained at boiling point of water ngineer M	Applie	
Coberly and	Air celite	Steam heated walls	70 - 300	Ke= 0.018+0.00098Rep
Marshall (1951)				
Colbum	Air pebbles,	Steam-jacketed	G:1-9	$h = 8aCpv^2G^{0.23}$
(1931)	granules, pellets,	packed tube		$a = f(D_P/D_t)$
	Porcelain balls, etc			
Furmas	Air – iron	Heated air	120 - 1200	$h = 6.91 X 10^{-3} X$
(1930)	spheres			$Gr^{0.75}t_fXG-1.75$
Gamson et.al	Air –celite	Water soaked packing	40 -4000	$J_h=1.064XRep^{0.41}$
(1943)	spheres dried			$Re>35; J_h = 1.81X$
	by air Cylinders			${\rm Re_{P}}^{-10}$; ${\rm Re_{P}} < 40$
Glasser and	Air – ceramic/	Transient heating by	330 - 1500	$Nu = 1.25 Re_P^{0.56}$
Thodos (1958)	brass spheres	regenerating technique Steady –state heating	300 - 4000	300 <rep<4000< td=""></rep<4000<>
Gupta and	Existing data	Electrical heating	33 - 6500	$\epsilon jh = 0.0108 +$
Thodos(1962a)	of single sphere		Re>20	$0.929/\text{Re}_{P}^{0.58}$
Gupta and	Air-celite	Water -soaked particles	95 - 2500	$\epsilon jh = 2.06/Re_{P}^{0.28}$
Thodos(1962b)	spheres	dried by air		
Houghen and Piret(1951)	Air – celite spheres bed	heated air entering the	193 – 2824	$\frac{K_e/C_P\mu = 3.7/\epsilon}{x(Re_P)^{1/3}}$



EAM			
Leva (1947)	Air –smoothHeated walls Spheres	500 - 3408	$h = 0.813 k_f/Dt$ e- ^{0.6(Dp/Dt)} Rep ^{0.9}
Leva and	Air – smooth Heated walls	500 - 3408	$h = 0.813 k_c$
Grummer	snharas	.7	n -0.013ki
(10.49)	spheres		
(1948)		250 2000	1 251 (D)
Leva <i>et.al</i>	Air smooth Heat air and Co_2	250 - 3000	$h = 3.5 K_{\rm f} / Dt$
(1948)	spheres bed wall is cooled		$D_{t.}e^{-0(DP/Dt)}Re_{P}^{0.7}$
Lindauter	Air – steel Electrical resistance 23 – 18200		
(1967)	and tungsten heating to produce		
	Sinusoidal gas Temperature		
Wakao and	Air glass concentric		$K/K_{c} = (K/k_{c})_{M} =$
Vato (1060)	arboroundum electric		$\Lambda_{e}/\Lambda_{f}^{-} = (\Lambda_{e}/\Lambda_{f})_{Nur}^{-}$
Kato (1909)			0+0.707
	Heater		$Nu_t^{and}(k_e/k_f)^{and}$
Yagi and	Air- iron/ Porcelain coaxial electric heater		
K _e /K _f =B+Re _P Pr _P ,			
Kunii (1957)	cement clinker, at the center, outside wall		
	fire brick and is insulated with fire brick		
	Raschig rings		
	Tubbing Tings		

IV. HEAT TRANSFER WITH NANO FLUIDS

The nanofluids show a superior potential for increasing heat transfer rates in a variety of cases. Different theories have been proposed to explain heat transfer enhancement. Early experiments with nanofluid for the determination of heat transfer coefficients have been undertaken by Pak and Cho [18] and Xuan and Li [26-27] in the turbulent Reynolds number range. They developed empirical correlations for the estimation of Nusselt number using nanofluids dispersed in water with TiO2, Al2O3 and CuO nanoparticles. The results indicate a remarkable increase in heat transfer coefficients compared to base fluid at the same Reynolds number. The nanofluids have shown an increase in heat transfer coefficient over that of water in the low volume concentration less than 1.0% undertaken.

Wen and Ding [24] measured the local heat transfer coefficients along the tube length during laminar flow. They conducted experiments with γ - Al2O3 nanofluid dispersed in water for forced convection in a copper tube of inner diameter 4.5mm and 970mm long. The correlation of Shah [19] for thermal entry length under constant heat flux is given by

$$Nu = 4.364 + 0.072 \left(\text{RePr} \frac{D}{x} \right)$$

for (RePrD/x) < 33.3 (19)

Nu = 1.95
$$\left(\operatorname{RePr} \frac{D}{x} \right)^{1/3}$$
 for $\left(\operatorname{RePr} D/x \right) \ge 33.3$ (20)

Most of the research investigated in this review paper was for laminar forced convection in a tube, with or without the packing material because there is very little research on forced convection in packed beds with nano fluids with different concentration. All of the research studied in this review paper reported increases in heat transfer due to the addition of nanoparticles in the base fluid. From the Figure 1.0 to Figure 4.0 the following conclusions are noted. The friction factor increases with lowering particle diameters and increasing concentration of the nanofluid. A regression equation is obtained for the estimation of friction factor with an average deviation of $\pm 0.08\%$ and standard deviation of 1.68%

$$f = 20.0593 R_{\rm p}^{-0.3117} (1+\varphi)^{0.2919}$$
(21)

A regression equation is developed for the estimation of Nusselt number as a function of particle Reynolds number, Prandtl and volume concentration of nanofluid. It is obtained with a standard deviation of 1.56% and an average deviation of -3.92% given by

$$Nu = 0.188 \text{Re}_p^{0.98} (1 + \phi)^{0.5310} \text{Pr}^{-0.4403}$$
 (22)

V. CONCLUSIONS

However, the following trends are in general agreement with all researchers

- (i) There is an enhancement in the heat transfer coefficient with increasing Reynolds number in packed beds
- (ii) The heat transfer coefficient increases with nanoparticle volume fraction.
- (iii) The heat transfer coefficient increases with fluid temperature, though not significant.
 - (iv) The heat transfer coefficient increases with the diameter of the packing material.
 - (v) There is enhancement of heat transfer coefficient with decreasing in void fraction.





0.8

1.0

(vi) The heat transfer coefficient changes with packing material properties.



0.4

0.6

0.2

bed length

0.0







Reynolds number

Nomenclature Constants

A, C constants	[-]			
Cp specific heat	[J/KgK]			
\overline{D} hydraulic diameter	[m]			
D diameter	[m]			
f friction factor	[-]			
G mass flow rate	[Kg/sec]			
g acceleration due to				
gravity				
g_c local acceleration due to	gravity			
h heat transfer coefficient	$[W/m^2]$			
h_v volumetric heat transfer				
coefficient	$[W/m^3]$			
I_0 Bessel's function of				
first kind []				
j colburn factor [J]				
k thermal conductivity	[W/mK]			
L length	[m]			
m, n constant [-]				
Nu Nusselt Number [-]			
PrPrandtl Number [-]				
Pe Peclet Number [-]				
T temperature [K]				
ΔP pressure drop [Pase	cal]			
Re Reynolds number [-]			
V velocity [m/sec]				
x axial distance [m]				
St Stanton number [-]				
xf tota <mark>l fri</mark> ctional fac	tion [Pascal]			
Δx disp <mark>la</mark> cement in as	xial distance[m]			
of t <mark>ot</mark> al pressure d	lrop			
Y constant [-]				
Z constant [-]				
Subcorinte				

Subscripts

April	superficial	
Dering	diameter	

- D fluid f
- W wall
- fi fluid inlet
- solid inlet Si
- Р particle
- effective radial er
- ef effective

Greek symbols

- non dimensional temperature [-] θ
- $[kg/m^3]$ density ρ
- 3 void fraction
- [N-sec/m] viscosity μ
- nano particle volume concentration [%] ф

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